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## Simulation and measurements of Geiger discharge transverse size in a SiPM cell.

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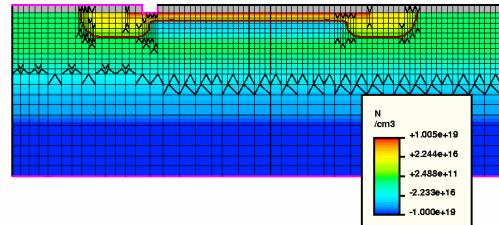
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*2-University of Kansas, USA*

*3-Max-Planck-Institute for Physics, Munich, Germany*

# Geiger discharge in a SiPM cell

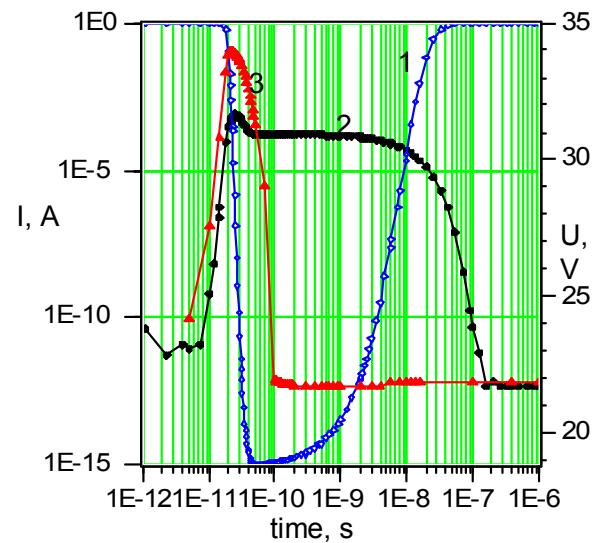
Example ISE TCAD simulation



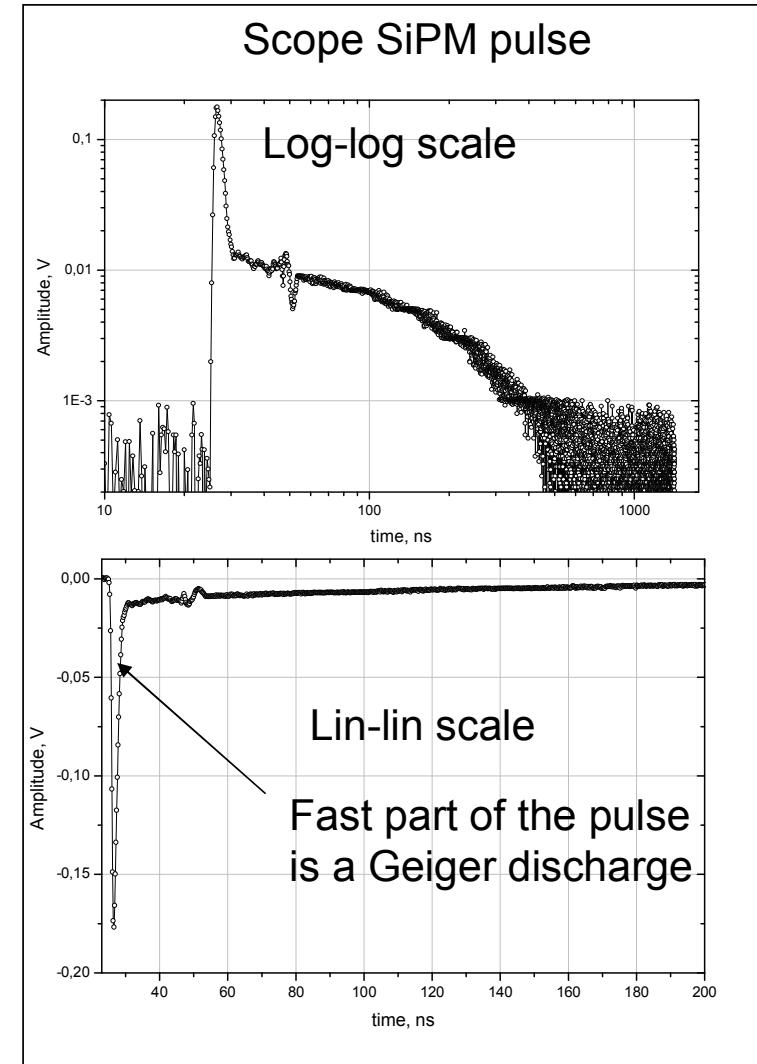
$$\nabla \cdot \epsilon \nabla \psi = -q(p - n + N_{D^+} - N_{A^-})$$

$$\nabla \cdot \overline{J_n} = qR + q \frac{\partial n}{\partial t},$$

$$-\nabla \cdot \overline{J_p} = qR + q \frac{\partial p}{\partial t}$$



1. voltage on pn-junction
2. Current through contacts
3. Current inside pn-junction



# Geiger discharge

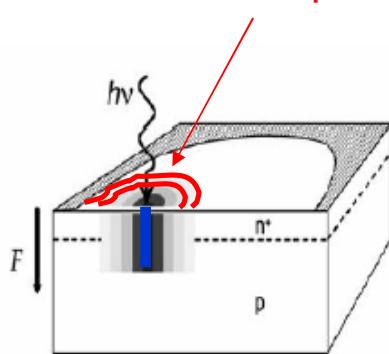
## SPAD Geiger discharge development

- A.Lacaita, et al."[Observation of avalanche propagation by multiplication assisted diffusion in p-n junction](#)" Appl.Phys.Lett. 57, 489-491 (1990)
- A.Lacaita, S.Cova et al."[Photon-assisted avalanche spreading in reach-through photodiodes](#)" Appl. Phys. Lett., 62, 606-608 (1993)
- A.Lacaita, et al.:"[Avalanche transients in shallow p-n junctions biased above breakdown](#)", Appl. Phys. Lett. 67, 2627-2629 (1995)
- A. Spinelli, A. Lacaita"[Physics and Numerical Simulation of Single Photon Avalanche Diodes](#)" IEEE Trans. Electron Devices, 44, 1931-1943 (1997)

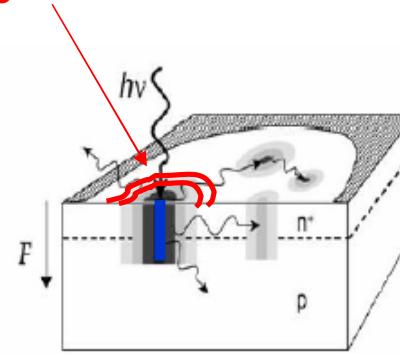
### Photon absorption

longitudinal build-up of avalanche process

transversal spreading of avalanche



Multiplication assisted diffusion



Photon assisted propagation

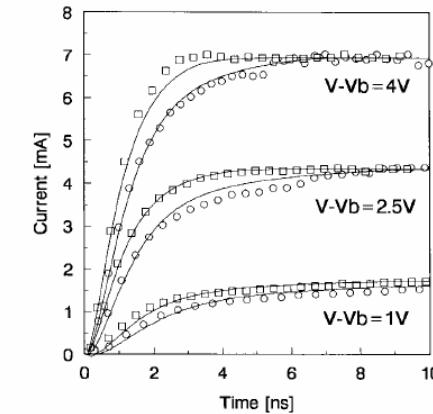
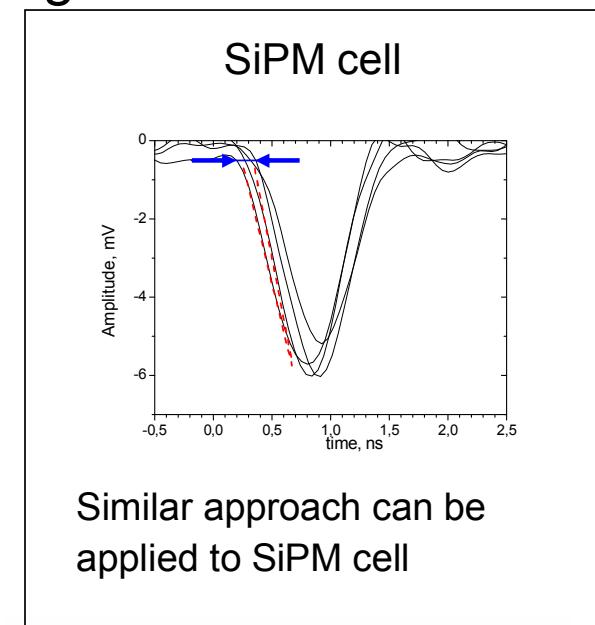


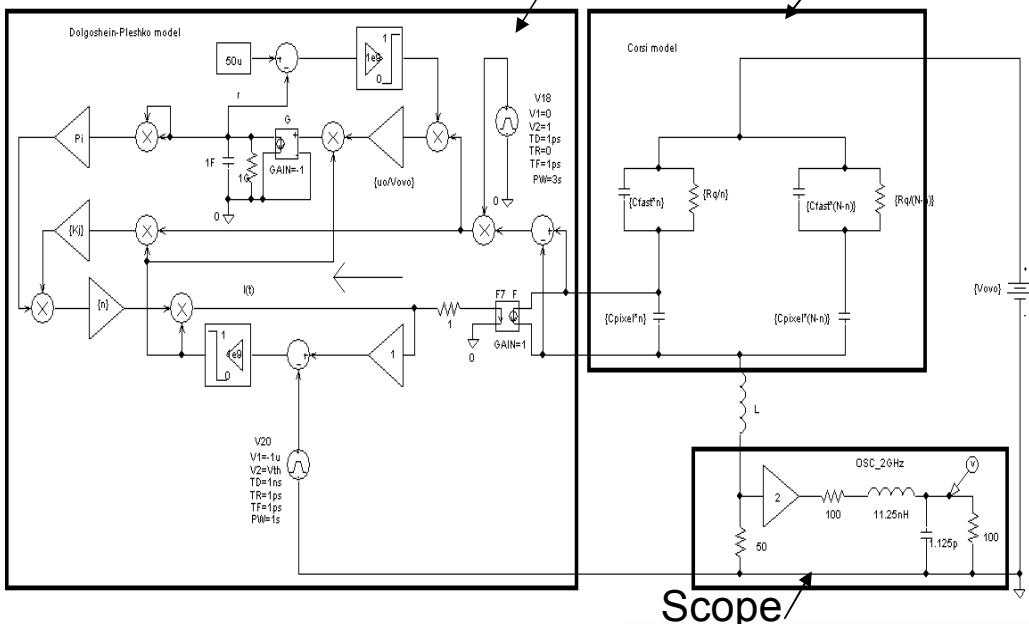
Fig. 18. Experimental data for avalanche triggered in the center of the active area (squares) and at one edge (circles). The solid lines are the corresponding simulation results. The active area of the SPAD is  $140 \times 14 \mu\text{m}$ .



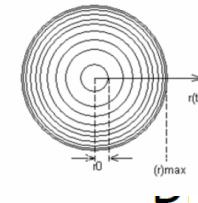
## Spice model of avalanche development in a SiPM cell (transversal propagation)

Transversal avalanche propagation &  
Avalanche current selfquenching

Dolgoshen-Pleshko model



Corsi model



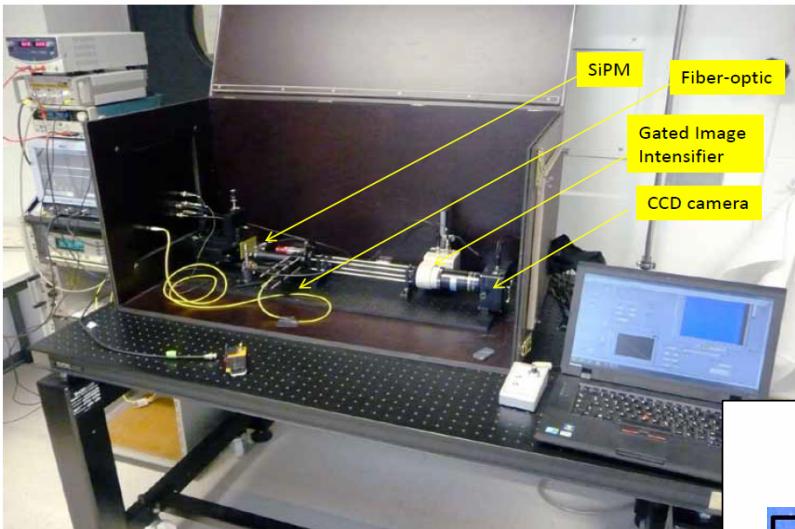
- Geiger discharge starts in a tiny spot inside a cell (1st disk)
- Current  $J(t)=K_j \cdot V_{ov}(t)$ , where  $K_j$  - is disk specific conductivity
- Discharge spreads from spot to 1st elementary ring, 2<sup>nd</sup>, ..., with velocity  $u(t) = u_0 \times V_{ov}(t)/V_{ov0}$ ,
- The capacitor of the cell discharges through the Geiger-avalanche current, after a while overvoltage drops down to 0

Scope

$V_{ov0}$ -initial overvoltage,  $V_{ov}(t)$  – momentary overvoltage  
 $K_j$ ,  $u_0$  - are experimental parameters

$$I(t) = J(t)S(t) = J(t) \times \pi r^2(t) = \pi k_j V_{ov}(t) \left[ \int_0^t u_0 \frac{V_{ov}(t')}{V_{ov0}} dt' \right]^2$$

## Light-Emission Microscopy (LEM) applied to SiPM



31 October2012, NSS & MIC,  
IEEE, Anaheim, CA, USA

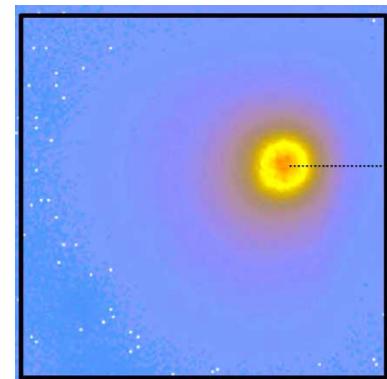
Razmik Mirzoyan, MPI for Physics: X-talk,  
Avalanche Size & Calibration of SiPM

laser 70 ps 405nm

Double Peltier element  
cooled low-noise CCD  
camera “CLARA” from  
ANDOR

Integration time ~600 s

### LEM Applied to Single SiPM Cell



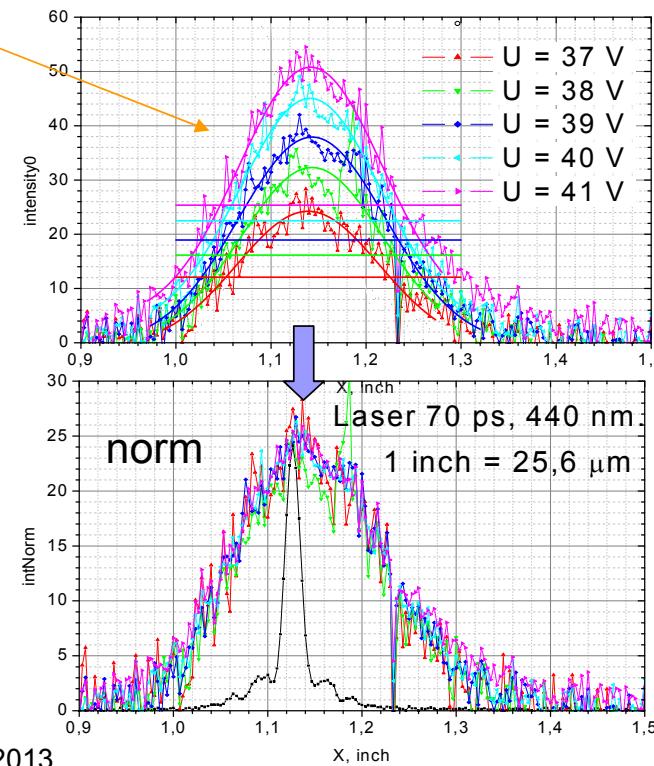
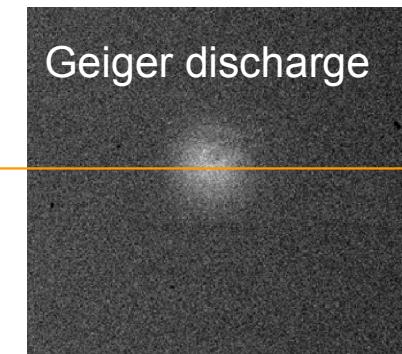
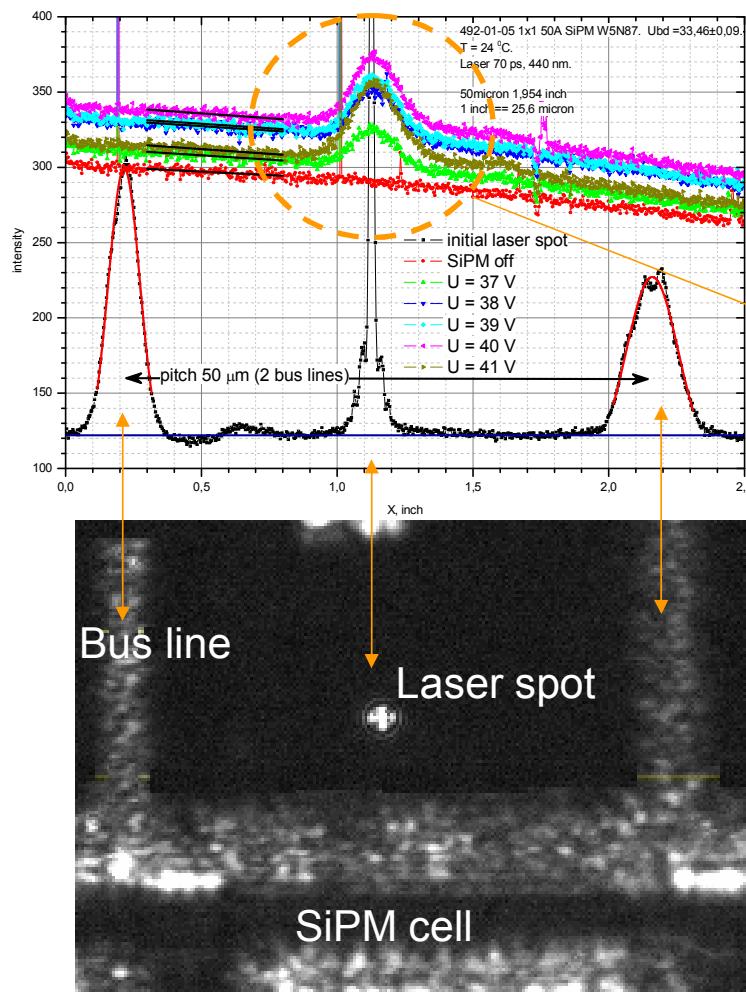
31 October2012, NSS & MIC,  
IEEE, Anaheim, CA, USA

Razmik Mirzoyan, MPI for Physics: X-talk,  
Avalanche Size & Calibration of SiPM

- Shooting with laser to a cell of  $100 \times 100 \mu\text{m}^2$  size
- The laser light is focused to a spot size of  $\sim 2 \mu\text{m}$
- Observing that the avalanche occupies only a small part of the cell

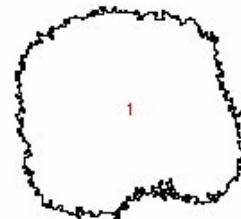
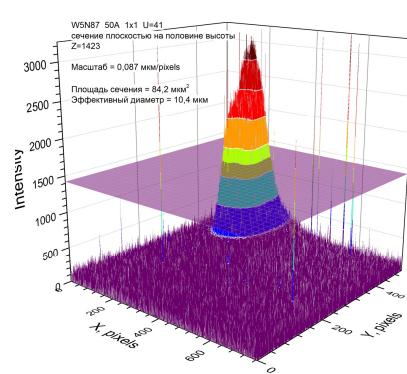


# Geiger discharge light

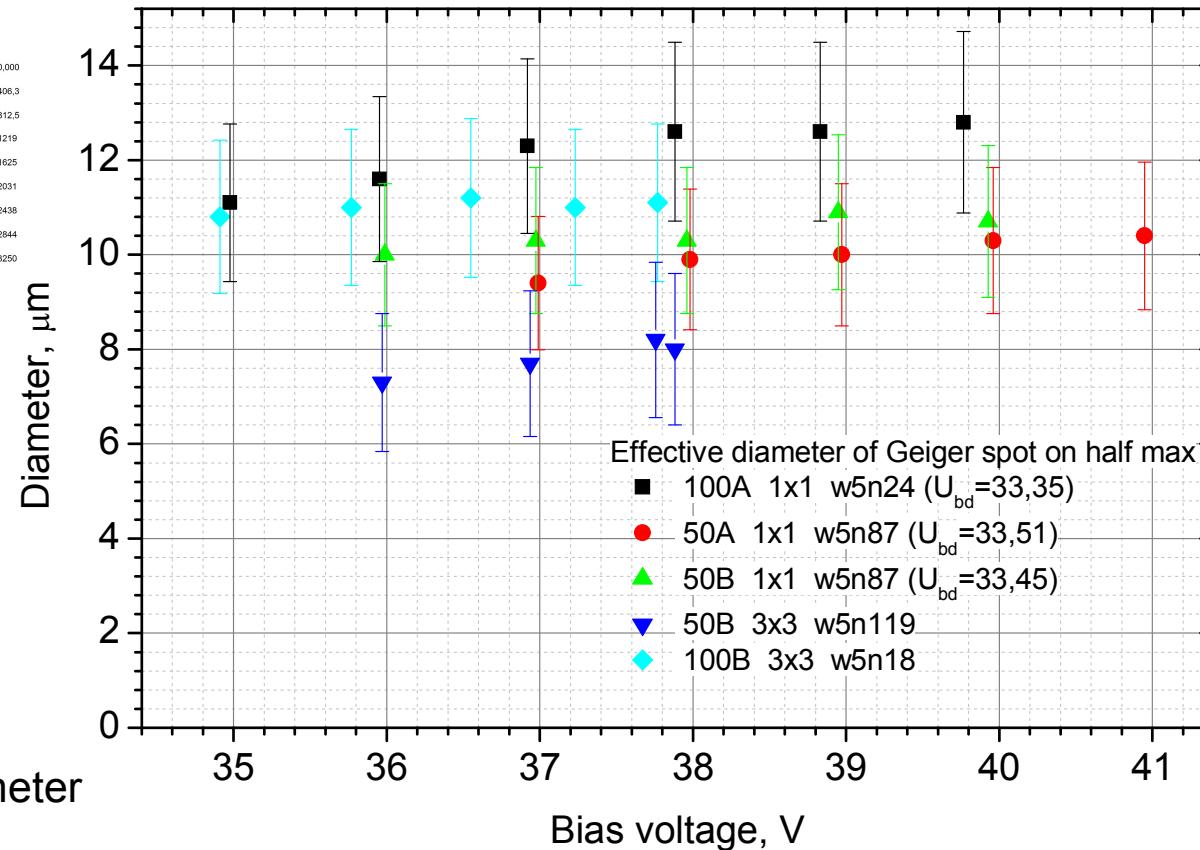




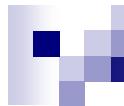
# Geiger discharge light



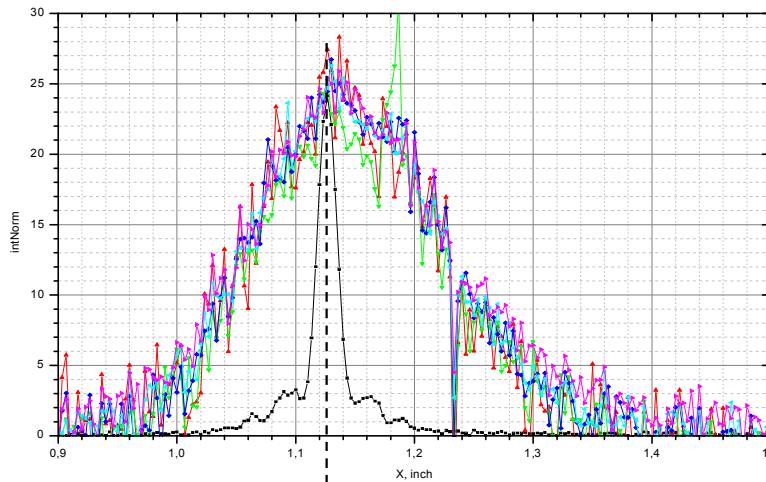
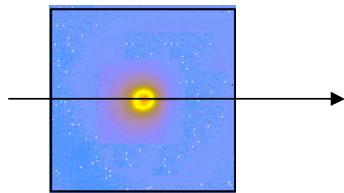
Area ->effective diameter



Spot size of Geiger discharge doesn't depend from overvoltage



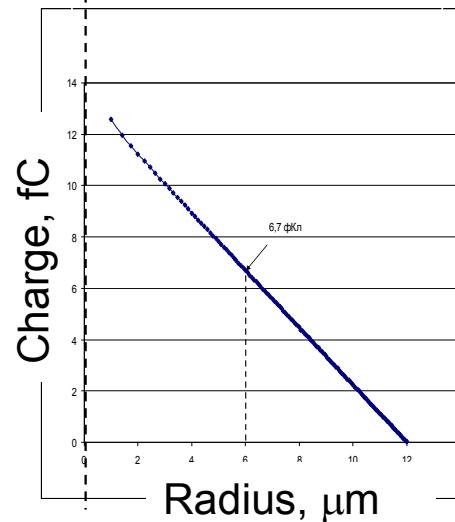
## Dolgoshin-Pleshko SPICE model

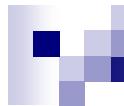


Light  
intensity

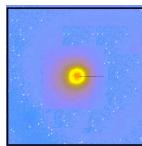
Geiger spot charge  
distribution.

Calculation on the basis  
of Dolgoshein-Pleshko  
SPICE model





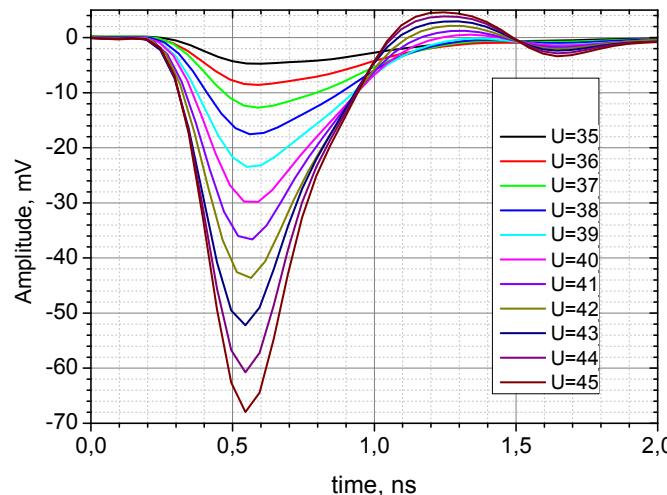
## SiPM cell study with digital oscilloscope LeCroy WaveRunner 620Zi 2GHz



### Width of the SiPM stand alone cell signals for different voltages

Focused laser beam into center of SiPM cell (pulse duration 40ps, 660nm)

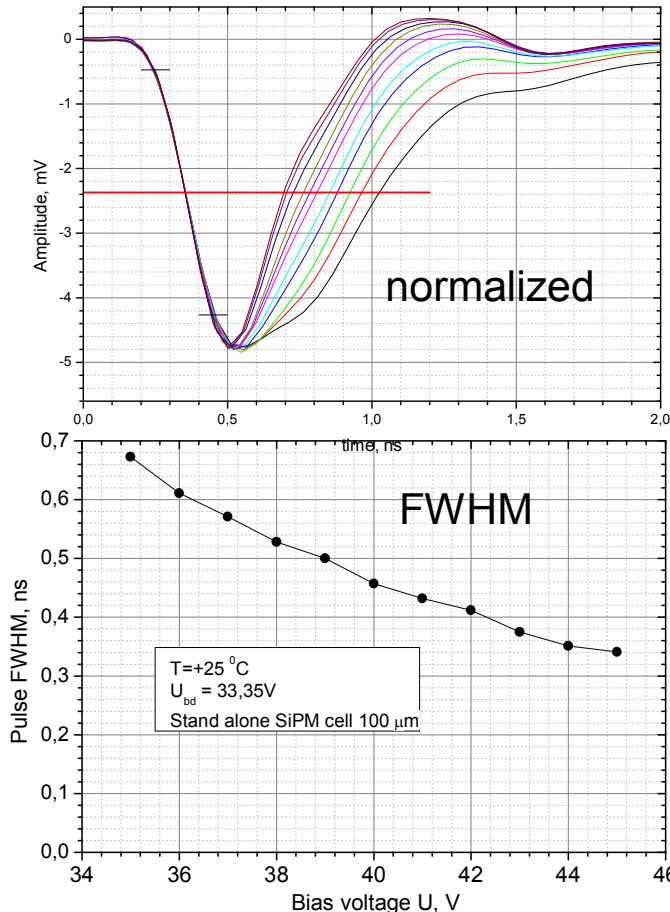
Average cell pulse for voltage range  
From  $U=35V$  to  $U=45V$  ( $U_{\text{Breakdown}} = 33.35V$ )



SiPM cell pulse width decreases with increasing of overvoltage

Charge Q from cell is proportional to applied overvoltage

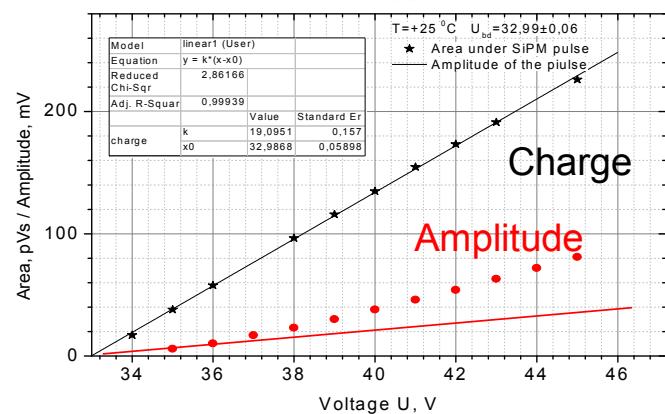
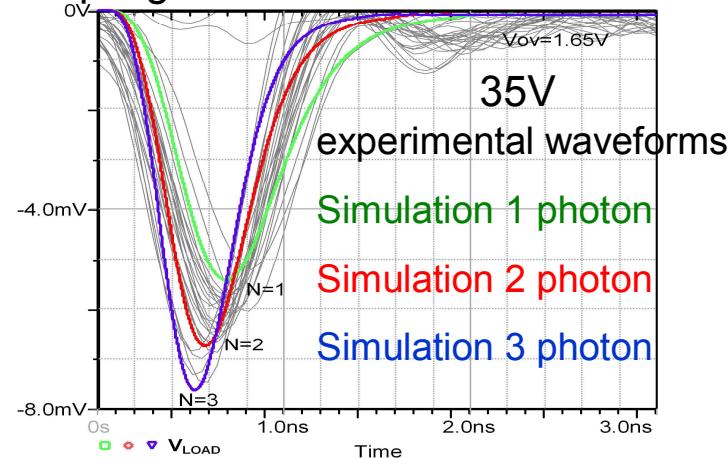
Amplitude grows faster then linear



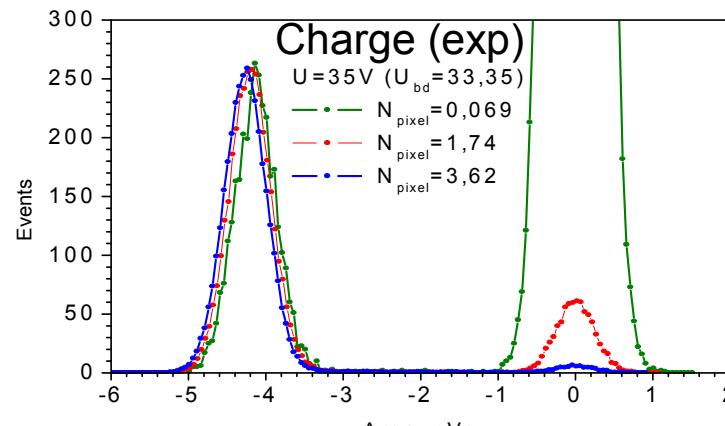
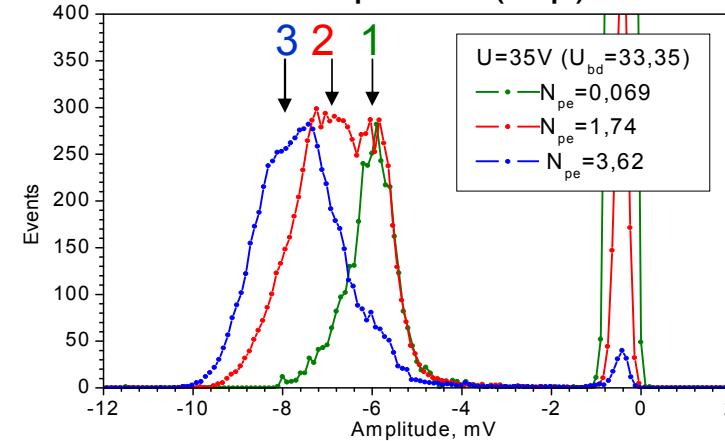
## Signals from stand alone cell

Fixed overvoltage  $\Delta U = 1.65V$ , different light intensity

### Exp signals & SPICE simulations



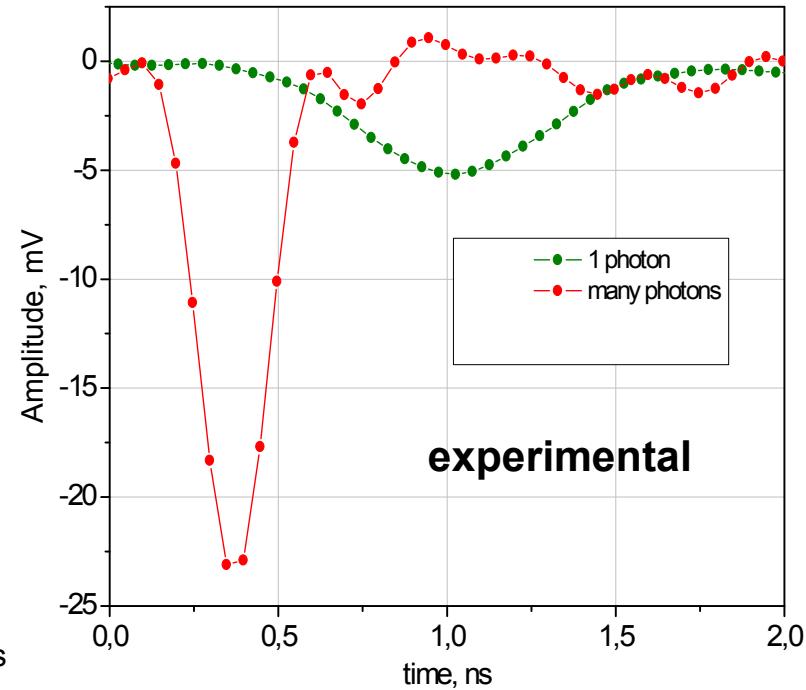
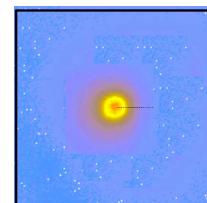
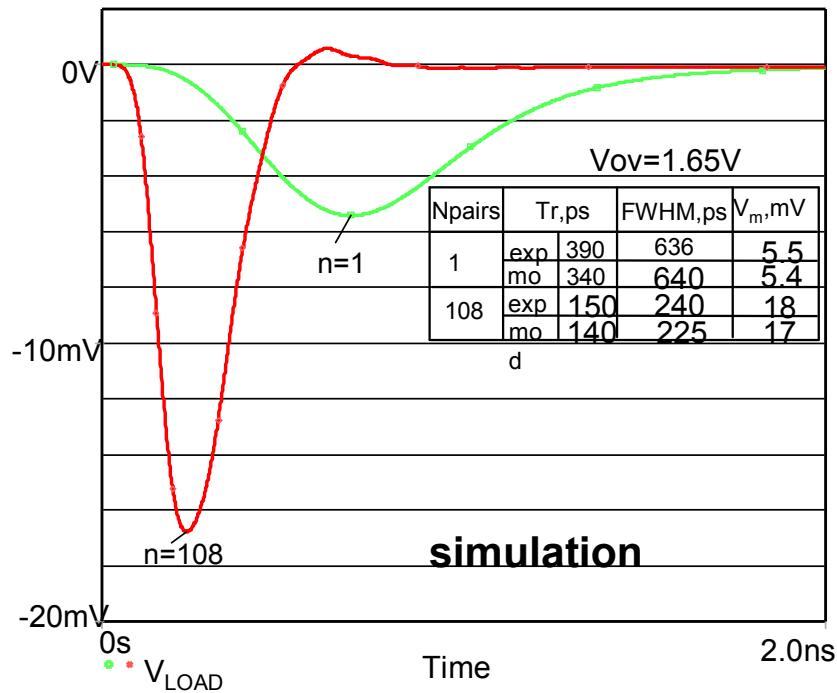
### Amplitude (exp)



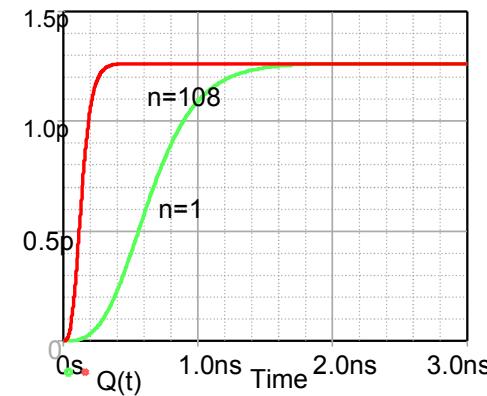
Even for very low light intensity we have “2-photons” amplitudes from cell -> it maybe an evidence of photon assisted discharge propagation

# Signals from stand alone cell.

Comparison of SPICE simulation and experimental results. Light of different intensity.

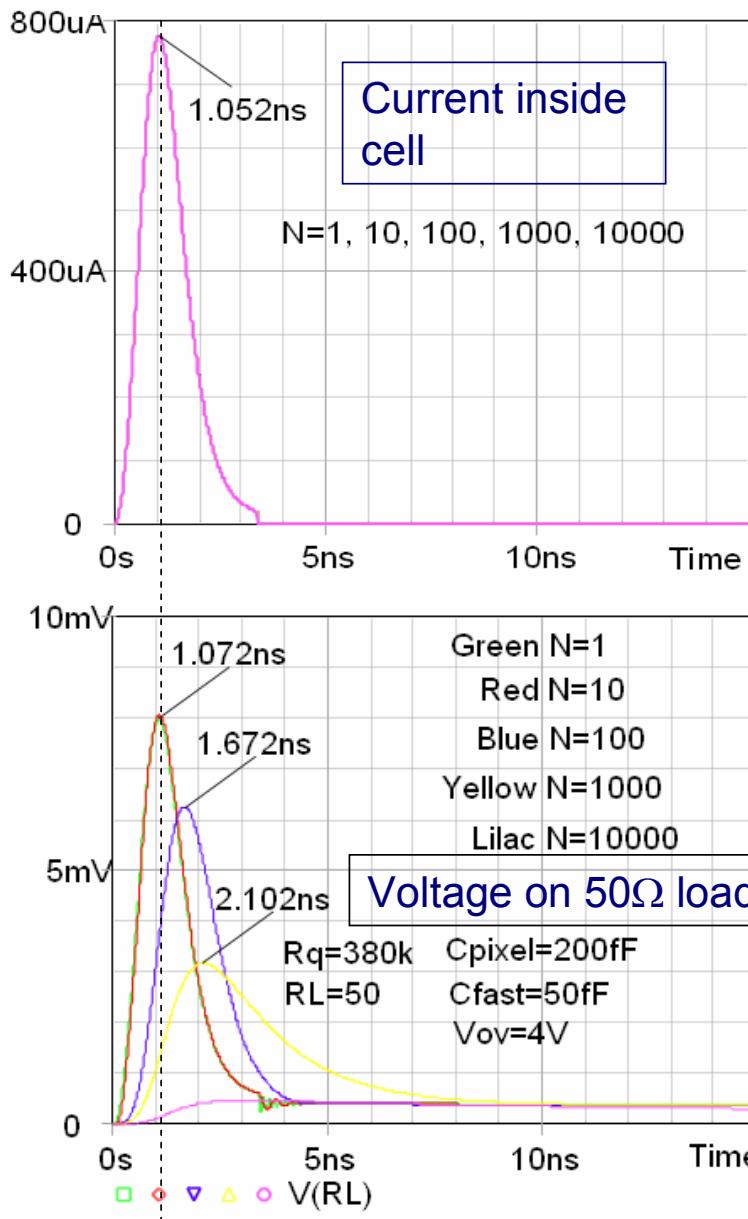


Simulation  
charge

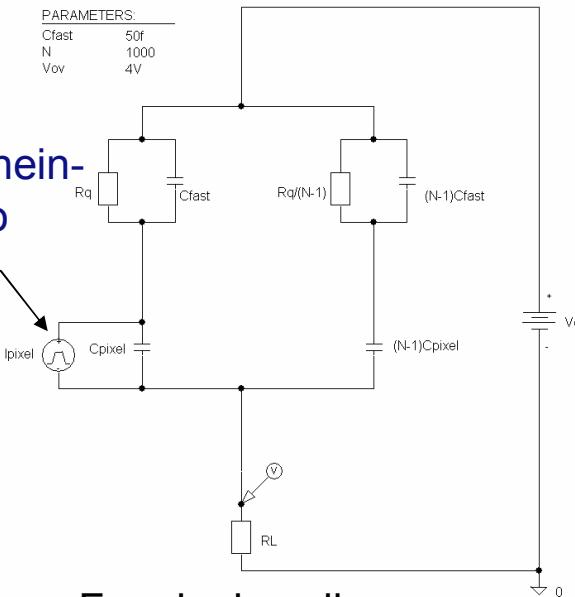


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## Different number of cells N inside SiPM



## SiPM SPICE model with Transversal current expansion



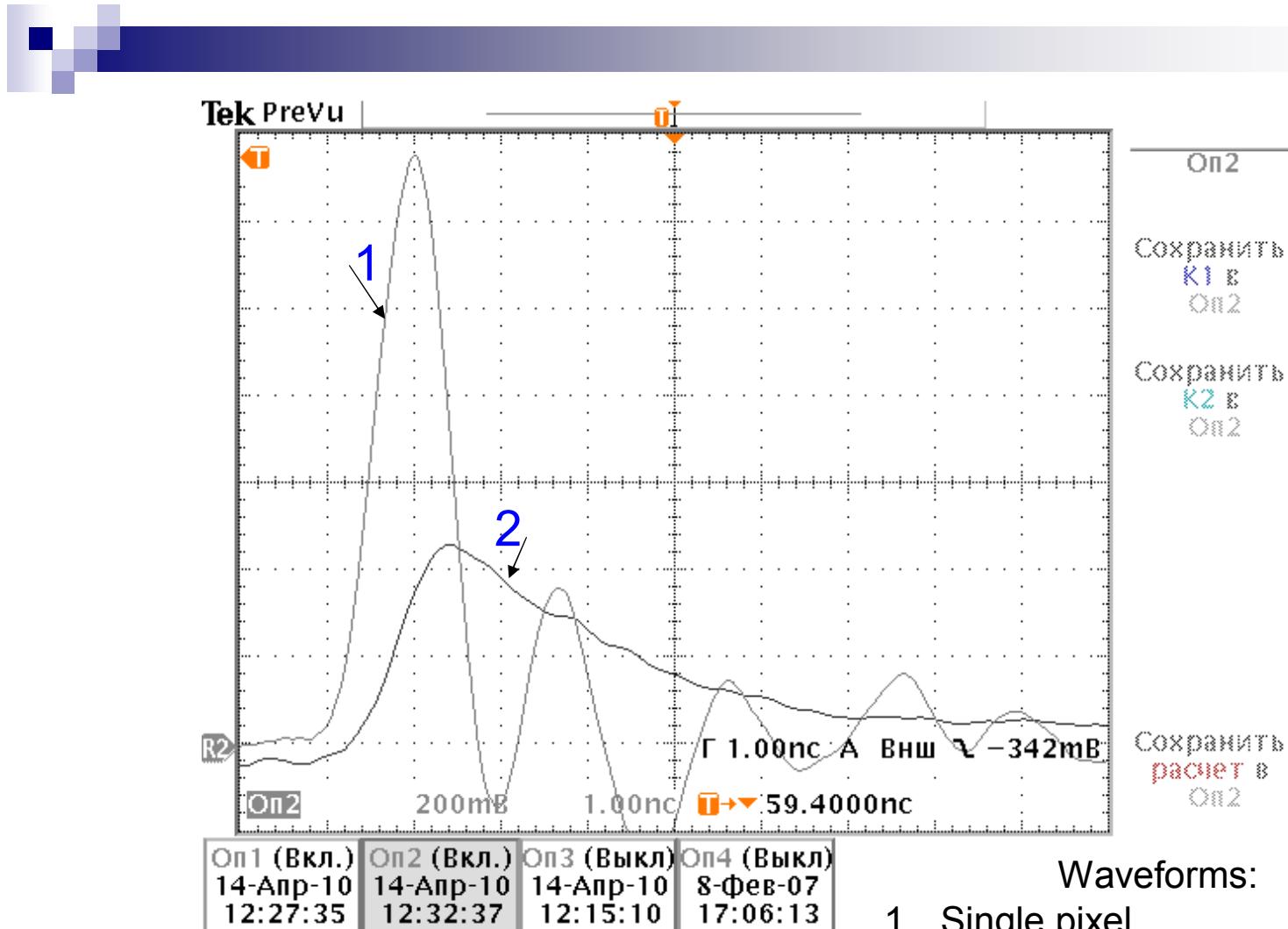
Dolgoshchein-  
Pleshko  
model

For single cell

$$I_{load} = [C_{fast}/(C_{fast} + C_{pixel})] * I_{inside}$$

$$I_{load} = 8mV/50\Omega = 160\mu A$$

With increasing total number of cells inside SiPM we decrease amplitude of single cell signal and obtain more slower pulse front



### Waveforms:

1. Single pixel
2. One pixel from 1x1mm<sup>2</sup> SiPM the same topology



## SUMMARY

- Geiger discharge inside the SiPM cell has a limited spot size at the level of 8-10 microns (Light Emission Microscope studies)
- Spot size of Geiger discharge doesn't depend on overvoltage
- Single SiPM cell pulse width decreases with overvoltage
- Spice model of transversal avalanche propagation & Geiger discharge self quenching in SiPM cell has been developed (Dolgoshin – Pleshko) on the basis of Light Emission Microscope studies and cell waveform analysis
- SPICE model nicely predict waveform of SiPM signals and can be useful for SiPM itself or FE electronics engineering.

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